

REVIEW FOR SPRING EXAM #1

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Use a calculator to approximate each to the nearest thousandth.

1) $\log_3 20$

Rewrite each equation in exponential form.

2) $\log_{14} b = a$

3) $\log_6 \frac{1}{216} = -3$

Rewrite each equation in logarithmic form.

4) $144^{\frac{1}{2}} = 12$

5) $x^{-12} = y$

Condense each expression to a single logarithm.

6) $10 \ln z + 10 \ln x - 5 \ln y$

7) $18 \log_9 u + 6 \log_9 v + 6 \log_9 w$

Expand each logarithm.

8) $\log_7 (uv^5)^5$

9) $\log_6 (y \cdot z \cdot w\sqrt{x})$

Identify the domain and range of each.

10) $y = \ln (x + 4)$

11) $y = \log (x - 2) - 3$

Find the inverse of each function.

12) $y = \log_x 4 - 4$

13) $y = \log_5 (x - 8)$

Solve each equation.

14) $\log_{12} (p^2 - p) = \log_{12} (35 + p)$

15) $\log_{15} (k^2 + 4k) = \log_{15} (10 + k)$

16) $\log_3 2 + \log_3 2x^2 = 4$

17) $\log_3 4 - \log_3 3x = \log_3 40$

18) $32^r = 16^{2r-1}$

19) $36^{3-3m} = 216^{2m}$

Simplify.

20) $(2y^2)^5$

21) $(2m^5n^5)^3$

Simplify. Your answer should contain only positive exponents with no fractional exponents in the denominator.

22) $(x^2)^{\frac{4}{3}}$

Simplify.

23) $\sqrt[3]{64x^4y^4z^6}$

24) $\sqrt[4]{64x^6y^7z^3}$

Approximate the relative minima and relative maxima of each function to the nearest tenth.

25) $f(x) = x^2 + 4x - 1$

26) $f(x) = -x^3 - 5x^2 - 8x - 8$

Simplify each expression.

27) $(7p^2 + 2 + 4p^4) + (4p - 4 - 7p^4)$

28) $(5r + 5r^3 - 4r^2) - (6r^2 + 6r^3 + 5r)$

Divide.

29) $(10x^2 + 33x - 28) \div (x + 4)$

Find all roots.

30) $5x^3 - 6x^2 + x = 0$

State the possible rational zeros for each function. Then find all zeros.

31) $f(x) = x^3 - 4x - 15$

32) $f(x) = 5x^3 - x^2 - 5x + 1$

Find all zeros.

33) $f(x) = x^4 + 5x^2 + 4$

34) $f(x) = x^3 + 5x^2 - 46x - 20$

35) $f(x) = 2x^3 - 3x^2 - 3x + 2$

Factor each.

36) $x^3 - 7x^2 + 10x = 0$

State if the given binomial is a factor of the given polynomial.

37) $(x^3 + 11x^2 + 15x - 27) \div (x + 9)$

38) $(x^3 + 20x^2 + 108x + 82) \div (x + 10)$

Write a polynomial function of least degree with integral coefficients that has the given zeros.

39) 2, 0, 3, -5

40) 2, 4, -i

Answers to REVIEW FOR SPRING EXAM #1

1) 2.727

2) $14^a = b$

3) $6^{-3} = \frac{1}{216}$

4) $\log_{144} 12 = \frac{1}{2}$

5) $\log_x y = -12$

6) $\ln \frac{z^{10} x^{10}}{y^5}$

7) $\log_9 (w^6 v^6 u^{18})$

8) $5 \log_7 u + 25 \log_7 v$

9) $\log_6 y + \log_6 z + \log_6 w + \frac{\log_6 x}{2}$

10) Domain: $x > -4$
Range: All reals

11) Domain: $x > 2$
Range: All reals

12) $y = 4^{\frac{1}{x+4}}$

13) $y = 5^x + 8$

14) $\{-5, 7\}$

15) $\{2, -5\}$

16) $\left\{\frac{9}{2}, -\frac{9}{2}\right\}$

17) $\left\{\frac{1}{30}\right\}$

18) $\left\{\frac{4}{3}\right\}$

19) $\left\{\frac{1}{2}\right\}$

20) $32y^{10}$

21) $8m^{15}n^{15}$

22) $x^{\frac{8}{3}}$

23) $4xyz^2 \sqrt[3]{xy}$

24) $2xy \sqrt[4]{4x^2 y^3 z^3}$

25) Minima: $(-2, -5)$
Maxima: None

26) Minima: $(-2, -4)$
Maxima: $(-1.3, -3.9)$

27) $-3p^4 + 7p^2 + 4p - 2$

28) $-r^3 - 10r^2$

29) $10x - 7$

30) $\left\{0, \frac{1}{5}, 1\right\}$

31) Possible rational zeros: $\pm 1, \pm 3, \pm 5, \pm 15$

Zeros: $\left\{3, \frac{-3 + i\sqrt{11}}{2}, \frac{-3 - i\sqrt{11}}{2}\right\}$

32) Possible rational zeros: $\pm 1, \pm \frac{1}{5}$

33) $\{2i, -2i, i, -i\}$

34) $\{5, -5 + \sqrt{21}, -5 - \sqrt{21}\}$

Zeros: $\left\{\frac{1}{5}, -1, 1\right\}$

35) $\left\{2, \frac{1}{2}, -1\right\}$

36) $x(x-2)(x-5) = 0$

37) Yes

38) No

39) $f(x) = x^4 - 19x^2 + 30x$

40) $f(x) = x^4 - 6x^3 + 9x^2 - 6x + 8$