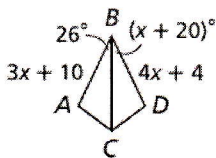


Section 5.1 (SSS and SAS)

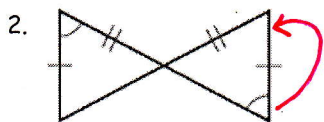
1. Show that $\triangle ABC \cong \triangle DBC$, when $x = 6$.



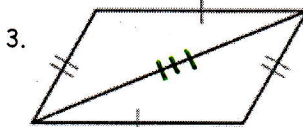
$BC \cong BC$ (Reflexive)
 $\angle ABC \cong \angle DBC$
 $26 = x + 20$
 $26 = 6 + 20 \checkmark$
 $AB \cong DB$
 $3x + 10 = 4x + 4$
 $3(6) + 10 = 4(6) + 4 \checkmark$

$\triangle ABC \cong \triangle DBC$
by SAS

Which postulate, if any, can be used to prove the triangle congruent?

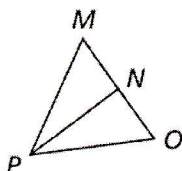


None, the angle would need to be between the two sides.



SSS

4. Given: \overline{PN} bisects \overline{MO} . $\overline{PN} \perp \overline{MO}$
Prove: $\triangle MNP \cong \triangle ONP$



Statements	Reasons
1. \overline{PN} bisects \overline{MO}	Given
2. $\overline{MN} \cong \overline{ON}$	Def. of Bisector
3. $\overline{PN} \cong \overline{PN}$	Reflexive POC
4. $\overline{PN} \perp \overline{MO}$	Given
5. $\angle PNM$ and $\angle PNO$ are right \angle s	Def. of Perpendicular Bisector
6. $\angle PNM \cong \angle PNO$	Right Angle Theorem
7. $\triangle MNP \cong \triangle ONP$	SAS

Options for Proof:

Definition of Perpendicular Bisector

Given

Reflexive POC

Definition of Bisector

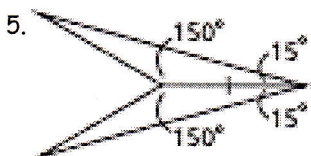
Given

SAS

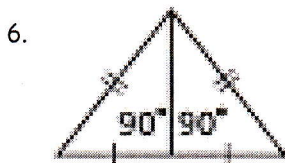
Right Angle Theorem

Section 5.2 (ASA, AAS, and HL)

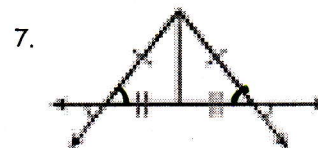
Identify the postulate or theorem that proves the triangles congruent.



ASA



HL

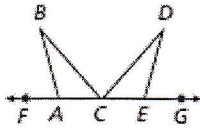


SSS or SAS

*Remember only works with right triangles.

8. Given: $\angle FAB \cong \angle GED$, $\angle ACB \cong \angle DCE$, $\overline{AC} \cong \overline{EC}$

Prove: $\triangle ABC \cong \triangle EDC$



* Supplementary: two \angle s add to get 180°

Statements	Reasons
1. $\angle FAB \cong \angle GED$	Given
2. $\angle BAC$ is a supplementary of $\angle FAB$. $\angle DEC$ is a supplementary of $\angle GED$	Def. of Supp. Angles
3. $\angle BAC \cong \angle DEC$	Cong. Supp. \angle s Theorem
4. $\angle ABC \cong \angle DCE$, $\overline{AC} \cong \overline{EC}$	Given
5. $\triangle ABC \cong \triangle EDC$	ASA

Options for Proof:

ASA

Definition of Supplementary Angles

Congruent Supplementary Angle Theorem

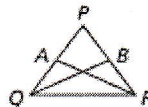
Given

Given

Section 5.3 (CPCTC)

9. Given: Isosceles $\triangle PQR$, base \overline{QR} , $\overline{PA} \cong \overline{PB}$

Prove: $\overline{AR} \cong \overline{BQ}$



Statements	Reasons
1. Isosceles $\triangle PQR$, base \overline{QR}	Given
2. $\overline{PQ} = \overline{PR}$	Def. of Isosc. Triangle
3. $\overline{PA} = \overline{PB}$	Given
4. $\angle P \cong \angle P$	Reflexive POC
5. $\triangle QPB \cong \triangle RPA$	SAS
6. $\overline{AR} = \overline{BQ}$	CPCTC

Options for Proof:

Reflexive POC

Given

SAS

Def. of Isosceles Triangle

Given

CPCTC

10. Use the given set of points to prove $\triangle DEF \cong \triangle GHJ$:

$D(-4, 4)$, $E(-2, 1)$, $F(-6, 1)$, $G(3, 1)$, $H(5, -2)$, $J(1, -2)$.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$DE \cong GH$$

$$DE = \sqrt{(-2 - (-4))^2 + (1 - 4)^2} = \sqrt{13}$$

$$GH = \sqrt{(5 - 3)^2 + (-2 - 1)^2} = \sqrt{13}$$

$$DF \cong GJ$$

$$DF = \sqrt{(-6 - (-4))^2 + (1 - 4)^2} = \sqrt{13}$$

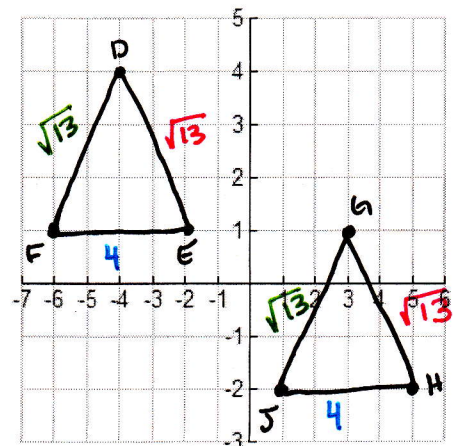
$$GJ = \sqrt{(1 - 3)^2 + (-2 - 1)^2} = \sqrt{13}$$

$$EF \cong HJ$$

$$EF = \sqrt{(-6 - (-2))^2 + (1 - 1)^2} = 4$$

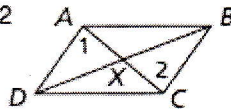
$$HJ = \sqrt{(-2 - 2)^2 + (1 - (-5))^2} = 4$$

$\triangle DEF \cong \triangle GHJ$
by SSS.



11. **Given:** X is the midpoint of \overline{AC} . $\angle 1 \cong \angle 2$

Prove: X is the midpoint of \overline{BD} .



Statements	Reasons
1. X is midpoint of \overline{AC} . $\angle 1 \cong \angle 2$	Given
2. $\overline{AX} = \overline{CX}$	Def. of Midpoint
3. $\overline{AX} \cong \overline{CX}$	Def. of \cong Segments
4. $\angle AXD \cong \angle CXB$	Vertical \angle s
5. $\triangle AXD \cong \triangle CXB$	ASA
6. $\overline{DX} \cong \overline{BX}$	CPCTC
7. $\overline{DX} = \overline{BX}$	Def. of \cong Segments
8. X is midpoint of \overline{BD}	Def. of Midpoint

Options for Proof:

CPCTC

Def. of Midpoint

Given

Def. of Congruent Segments

Def. of Midpoint

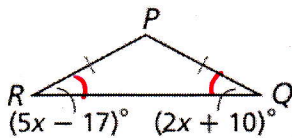
ASA

Vertical Angles

Def. of Congruent Segments

Section 5.4 (Isosceles and Equilateral Triangles)

Find each angle measure.



1. $m\angle R$

$\angle R = \angle Q$

$5x - 17 = 2x + 10$

$3x = 27$

$x = 9 \rightarrow \angle R = 28^\circ$

2. $m\angle P$

$\angle P + \angle R + \angle Q = 180$

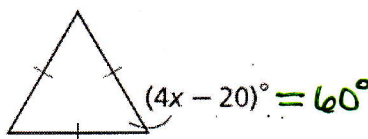
$x + 28 + 28 = 180$

$x + 56 = 180$

$x = 124^\circ \rightarrow \angle P = 124^\circ$

Find each value.

3. x

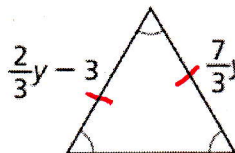


$4x - 20 = 60$

$4x = 40$

$x = 10$

4. y

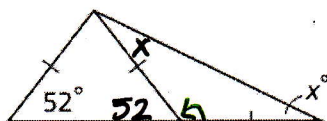


$\frac{2}{3}y - 3 = \frac{7}{3}y - 13$

$10 = \frac{5}{3}y$

$6 = y$

5. x



$180 - 52 = 128$

$128 + x + x = 180$

$128 + 2x = 180$

$2x = 52$

$x = 26$