

AIG Circles Homework

Name: KEY

1. What is the definition of a circle?
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2. What is the standard equation for a circle? $x^2 + y^2 = r^2$

3. What is the standard equation for a translated circle? $(x-h)^2 + (y-k)^2 = r^2$

Write the standard equation for each circle. Then state the coordinates of its center and give its radius.

5. $x^2 + y^2 + 4y = 12$

$$x^2 + (y^2 + 4y + 4) = 16$$

$$\boxed{x^2 + (y+2)^2 = 16}$$

$$c(0, -2) \quad r=4$$

6. $x^2 - 2x + y^2 = 8$

$$(x^2 - 2x + 1) + y^2 = 9$$

$$\boxed{(x-1)^2 + y^2 = 9}$$

$$c(1, 0) \quad r=3$$

7. $x^2 + 2x + y^2 + 2y = 2$

$$(x^2 + 2x + 1) + (y^2 + 2y + 1) = 2 + 1 + 1$$

$$\boxed{(x+1)^2 + (y+1)^2 = 4}$$

$$c(-1, -1) \quad r=2$$

8. $x^2 + 2x + y^2 + 6y = 6$

$$(x^2 + 2x + 1) + (y^2 + 6y + 9) = 6 + 1 + 9$$

$$\boxed{(x+1)^2 + (y+3)^2 = 16}$$

$$c(-1, -3) \quad r=4$$

9. $x^2 + y^2 - 10x - 2y = 23$

$$(x^2 - 10x + 25) + (y^2 - 2y + 1) = 23 + 1 + 9$$

$$\boxed{(x-5)^2 + (y-1)^2 = 49}$$

$$c(5, 1) \quad r=7$$

10. $x^2 + y^2 - 12x + 6y = 19$

$$(x^2 - 12x + 36) + (y^2 + 6y + 9) = 19 + 1 + 36$$

$$\boxed{(x-6)^2 + (y+3)^2 = 64}$$

$$c(6, -3) \quad r=8$$

11. $x^2 + y^2 + 6x - 17 = 0$

$$(x^2 + 6x + 9) + (y^2) = 26$$

$$\boxed{(x+3)^2 + y^2 = 26}$$

$$c(-3, 0) \quad r=\sqrt{26}$$

12. $x^2 + y^2 - 20y + 19 = 0$

$$(x^2 + y^2 - 20y + 100) = 81$$

$$\boxed{x^2 + (y-10)^2 = 81}$$

$$c(0, 10) \quad r=9$$

13. $x^2 + y^2 + x + y = 0$

$$(x^2 + x + 1/4) + (y^2 + y + 1/4) = 1/2$$

$$\boxed{(x+1/2)^2 + (y+1/2)^2 = 1/2}$$

$$c(-1/2, -1/2) \quad r=\sqrt{1/2}$$

State whether the equation is a parabola or a circle. Identify the vertex if it is a parabola and the center/radius if it is a circle.

14. $y = x^2$

Parabola

$$\boxed{v(0, 0)}$$

15. $x^2 = 12 - y^2$

Circle $\rightarrow x^2 + y^2 = 12$

$$\boxed{c(0, 0) \quad r=\sqrt{12}}$$

16. $x^2 = 4 - (y-2)^2$

Circle $\rightarrow x^2 + (y-2)^2 = 4$

$$\boxed{c(0, 2) \quad r=2}$$

17. $(y+2)^2 = 15 - (x-2)^2$

Circle $\rightarrow (x-2)^2 + (y+2)^2 = 15$

$$\boxed{c(2, -2) \quad r=\sqrt{15}}$$